

10. Exercise sheet for Numerik für Differentialgleichungen auf Oberflächen

Exercise 23*. Consider the surface evolution described by

$$\begin{aligned} v(x, t) &= -H(x, t)v_{\Gamma(X)}(x, t), \\ \frac{d}{dt}X(p, t) &= v(X(p, t), t), \\ X(p, 0) &= \text{Id}. \end{aligned}$$

Using the identity $-Hv_{\Gamma(X)} = \Delta_{\Gamma(X)}x_{\Gamma(X)}$, where $x_{\Gamma(X)}$ denotes the identity map on $\Gamma(X)$, derive the weak formulation of the problem.

Discretise the problem using evolving surface finite elements and linearly implicit BDF methods, then implement the resulting scheme.

* Solved together in the tutorial (*Präsenzaufgabe*).

Please, bring your laptops along!